

02913 Advanced Analysis Techniques

QuickCheck, the 2017 edition

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DTU Compute

Introduction (1/2)

In the next 3 weeks, you will learn

- the principles and practice of QuickCheck
- the OCaml programming language

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Why OCaml?

- QuickCheck is based on testing **properties**
- These are most easily expressed in a functional language such as OCaml, which has roots in mathematics and logic
- You can still QuickCheck software written in other languages
- Once we agree on the involved concepts you get to study other QuickCheck frameworks

Introduction (2/2)

We will focus on learning **concepts** rather than **products**

The QuickCheck concepts we will cover are **language independent**

The functional programming concepts we will need are **also universal**:

- they are as relevant to F#, Haskell, Standard ML, . . .
- they may come in handy next time you program, e.g., callbacks in JavaScript.

Practicalities

The course will consist of

- lectures (mornings)
- exercises (afternoons)
- a course project
- a project report
- a project presentation (end of week 3)

You'll receive a combined grade for the report+presentation.

Measure of success: apply QuickCheck and the covered techniques to a project of your choice

Outline

- Today we'll spend on preliminaries (getting OCaml working, etc)
- Over the next days we'll gradually learn QuickCheck (and OCaml) through lectures and exercises
- Guest lecture (week 2): Jesper Louis Andersen (does QuickCheck in the “real world”)
- Start thinking about a project topic
 - test an app,
 - test a webserver,
 - test a compiler,
 - ...

OCaml Basics

OCaml, botanically

- OCaml is a functional language (opposed to OO)
 - Functions are first class citizens (like in JavaScript, F#)
 - The core syntactic category is the expression (opposed to statements)
 - Assignments are possible, but rare
- OCaml is statically and **strongly** typed
 - No NullPointerExceptions, no ClassCastException
 - actually no casts at all!
 - Since everything is an expression, everything has a type
- The interpreter **infers** types automatically
 - Variables are (mostly) declared without an explicit type

Riding the Camel

OCaml comes with a read-eval-print loop (like Python):

```
$ ocaml
      OCaml version 4.02.3

# print_endline "hello, world!";;
hello, world!
- : unit = ()
#
```

All interaction must end with two semicolons

Basic Types (1/4)

OCaml comes with a number of base types:

`int`, `char`, `bool`, `string`, `float`, ...

- Integers are 63 bits for a 64-bit OCaml (and 31 bits for a 32-bit OCaml): `-1`, `0`, `1`, `42`, `max_int`, ... all have type `int`
- `ints` come with the usual arsenal of operations:
`+`, `-`, `*`, `/`, `mod`, `land`, `lor`, `lxor`, ...

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- `ints` come with the usual arsenal of operations:
`+`, `-`, `*`, `/`, `mod`, `land`, `lor`, `lxor`, ...
- Both 64-bit and 32-bit integers are also available:
 - `-1L`, `0L`, `1L`, ... all have type `int64` and come with separate operations: `Int64.add`, `Int64.sub`, `Int64.div`, ...
 - `-1l`, `0l`, `1l`, ... all have type `int32` and also come with separate operations: `Int32.add`, ...

Basic Types (2/4)

OCaml comes with

- **Booleans:** `true` and `false` have type `bool`
 - Negation is `not`, conjunction is `&&`, and disjunction is `||`
 - The usual comparison operations also produce booleans: `=`, `<>`, `<`, `<=`, `>`, `>=`, ...
- **Characters:** `'a'`, `'X'`, `'\n'`, `'\\'`, `'\012'`, ...
 - all have type `char`
 - One can convert back and forth with `char_of_int` and `int_of_char`

Basic Types (3/4)

OCaml comes with strings:

- `" "` and `"hello, _world!"` have type `string`
- String concatenation is `^`: `"029" ^ "13"`
- One can inspect and manipulate strings:
`String.length`, `String.uppercase`,
`String.lowercase`, ...
- And convert to and from strings: `int_of_string`,
`string_of_int`, `Int64.of_string`,
`Int32.to_string`, `bool_of_string`,
`string_of_bool`, ...

Basic Types (4/4)

- `()` has the type `unit`
- Notice how `println` returned `unit`
- `unit` serves the purpose of `void` in C and Java
- and doubles as the “empty argument (list)”:
`println()`
- Technically (or pedantically) it is not the “empty type” since one value has `unit` type, namely `()`
- `(* Comments are enclosed in
parentheses and asterisks *)`

Conditionals

Conditionals in OCaml are expressions and hence have a type:

```
if (1=2) || true then 1+3 else 42
```

As a consequence the two branches have to return something of the same type:

```
# if not false then "hello" else ();;
```

```
Error: This expression has type unit  
but an expression was expected of  
type string
```

```
#
```

OCaml, recap

- So far we've written some basic OCaml expressions following the below grammar:

$exp ::= value$ (ints, bools, chars, strings,...)
| $exp + exp$ | $exp - exp$ | ... (binary operations)
| $- exp$ (unary minus)
| (exp) (parenthesized exps)
| $id exp$ (function calls)
| **if** exp **then** exp **else** exp (conditionals)

Top-level let bindings

- In ML one can bind the value of an expression to a name:

```
let id = exp
```

For example:

```
let x = 3;;  
let y = 4;;  
x + y;;
```

- Important note: **this is not an assignment!**
- An assignment has state, i.e., a little piece of memory that can (and will) change under your feet...

Nested let bindings

- One can also locally bind a value to a name locally within an expression:

```
let id = exp in exp
```

- Confusingly this is also expressed with the **let** keyword(!)

For example:

```
let x = 3 in x * x * x
```

gives 27 but afterwards `x` is no longer visible:

```
# x+x;;
```

```
Error: Unbound value x
```

OCaml syntax, recap

A grammar can formally distinguish top-level **lets** from the nested, expression-level **lets**:

$$\begin{aligned} \textit{topdecl} ::= & \textit{exp} \\ & | \mathbf{let} \textit{id} = \textit{exp} \qquad \qquad \qquad \text{(top-level let)} \end{aligned}$$
$$\begin{aligned} \textit{exp} ::= & \textit{id} \\ & | \textit{value} \\ & | \textit{exp} + \textit{exp} \quad | \quad \textit{exp} - \textit{exp} \quad | \quad \dots \quad | \quad - \textit{exp} \\ & | (\textit{exp}) \\ & | \textit{id} \textit{exp} \\ & | \mathbf{if} \textit{exp} \mathbf{then} \textit{exp} \mathbf{else} \textit{exp} \\ & | \mathbf{let} \textit{id} = \textit{exp} \mathbf{in} \textit{exp} \qquad \qquad \qquad \text{(expr-level let)} \end{aligned}$$

Functions (are fun) (1/2)

Functions are written with the **fun** keyword:

```
fun id ... id -> exp
```

For example: **fun** x -> x * x

has the type: int -> int

We can bind the function value to a name:

```
let square = fun x -> x * x
```

and call it:

```
# square 4;;  
- : int = 16  
#
```

Functions (are fun) (2/2)

It is so common to bind a function value to a name that there is a short hand notation:

```
let funname id ... id = exp
```

For example: **let** square x = x * x

One can also locally define functions with similar short hand notation:

```
let funname id ... id = exp in exp
```

For example:

```
let quadruple n =  
  let double m = m + m in  
  double (double n)
```

Recursive functions

Recursive functions are explicitly marked as such with the `rec` keyword:

```
let rec funname id ... id = exp
```

For example:

```
let rec fac n =  
  if n = 0  
  then 1  
  else n * fac (n - 1)
```

To which OCaml responds:

```
val fac : int -> int = <fun>
```

Mutually recursive functions

Recursive functions that call each other should be declared simultaneously with **and**.

For example:

```
let rec is_even n =  
  if n = 0  
  then true  
  else is_odd (n - 1)  
and is_odd n =  
  if n = 0  
  then false  
  else is_even (n - 1)
```

to which OCaml responds:

```
 val is_even : int -> bool = <fun>  
val is_odd : int -> bool = <fun>
```

Pattern matching (1/5)

One typically destructs data using pattern matching:

```
match exp with  
  | pattern -> exp  
  | pattern -> exp  
  | ...
```

For example:

```
let bool_to_string b = match b with  
  | true    -> "true"  
  | false  -> "false"
```

Pattern matching (2/5)

OCaml's pattern matching compiler helps ensure that you don't miss a case:

```
let is_valid_bool s = match s with  
  | "true" -> true  
  | "false" -> true
```

Pattern matching (2/5)

OCaml's pattern matching compiler helps ensure that you don't miss a case:

```
let is_valid_bool s = match s with
  | "true" -> true
  | "false" -> true
```

Warning 8: this pattern-matching is not exhaustive.

Here is an example of a value that is not matched:

```
""
val is_valid_bool : string -> bool = <fun>
```

Pattern matching (3/5)

The wildcard pattern can be used to catch “default” behavior:

```
let is_valid_bool s = match s with  
  | "true"    -> true  
  | "false"   -> true  
  | _         -> false
```

which will satisfy OCaml:

```
val is_valid_bool : string -> bool = <fun>
```

The exhaustiveness check is your friend.

Don't use wildcards everywhere just to “make it shut up”.

Pattern matching (4/5)

Beware that the pattern order now matters:

```
let is_valid_bool s = match s with  
  | _           -> false  
  | "true"     -> true  
  | "false"    -> true
```

Pattern matching (4/5)

Beware that the pattern order now matters:

```
let is_valid_bool s = match s with  
  | _           -> false  
  | "true"      -> true  
  | "false"     -> true
```

Warning 11: this match case is unused.

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```
val is_valid_bool : string -> bool = <fun>
```

Pattern matching (5/5)

Patterns can also bind variables which will be visible within the pattern's right-hand-side:

```
let rec fac n = match n with  
  | 0 -> 1  
  | n -> n * fac (n - 1)
```

to which OCaml (again) responds:

```
val fac : int -> int = <fun>
```

Install OCaml and dive in

- The community homepage is `http://ocaml.org/`
- The standard OCaml distribution comes with, e.g,
 - a bytecode interpreter (`ocamlc`), a native code compiler (`ocamlopt`), a build tool (`ocamlbuild`) and a standard library:

`http://caml.inria.fr/pub/docs/manual-ocaml/libref/`

- There is even a (separately available) compiler to JavaScript (`js_of_ocaml`)
- I recommend ‘Introduction to Objective Caml’ by Jason Hickey, available at:

`http://courses.cms.caltech.edu/cs134/cs134b/book.pdf`

We will only need the first 12 chapters (~130 pages)

Editing OCaml code

IDE-wise, for

- **emacs** I recommend tuareg-mode
- **Eclipse** people recommend: OCaIDE
<http://www.algo-prog.info/ocaide/>
<http://pl.cs.jhu.edu/pl/ocaml/ocaide.shtml>
- **IntelliJ**: intellij-ocaml?
- **VIM**: OMLet
- **_**: please share your findings

These modes provide syntax highlighting.

Merlin: <https://github.com/ocaml/merlin>
provides online type-checking and context-sensitive
completion for emacs/vim/Atom/...

QuickCheck

Testing

Testing (either by hand or by a hand-written test suite)

- requires discipline and
- involves repetitive tasks

Claim: Computers are **much better**

- at discipline and
- repetitive tasks

than humans

So let the computers aid us!

QuickCheck (1/2)

QuickCheck combines two key ideas:

- random testing (random input) and
- specifications as oracles (property-based)

For this reason it is also called

randomized property-based testing

It was conceived by Koen Claessen and John Hughes around 1999 (published in 2000).

Initially as a Haskell library, since then ported to most other languages

QuickCheck (2/2)

The QuickCheck approach has since grown out of academia and into industry:

John Hughes and friends formed 'Quviq AB' which

- produces an Erlang QuickCheck library and
- sells QuickCheck consultancy.
- **see** `http://quviq.com/`

It has since been used, e.g., to test compatibility of AUTOSAR components for Volvo.

Both Hughes and our guest lecturer Jesper Louis Andersen uses QuickCheck to test **distributive systems**

QuickCheck, briefly

QuickCheck builds on the idea of expressing
a family of tests by

- a property of interest, e.g., $\forall n. (\text{fac } n) \bmod n = 0$
- a generator of arbitrary elements
 $0, 42, -2, 7234, -1000000, \dots$

QuickCheck, briefly

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and then have the property checked on, e.g., 100
arbitrary inputs.

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and then have the property checked on, e.g., 100
arbitrary inputs.

Bonus: you get to program, not really write tests :-)

Risk: you may make a programming error in the
property :-)

Garbage in, garbage out (also for QuickCheck)

On two occasions I have been asked, – *“Pray, Mr. Babbage, if you put into the machine wrong figures, will the right answers come out?”* In one case a member of the Upper, and in the other a member of the Lower, House put this question. I am not able rightly to apprehend the kind of confusion of ideas that could provoke such a question.

– Charles Babbage, 1864

This also applies to QuickCheck tests:

generators and **properties**

 Q: Can you think of a poor example of each?

QuickCheck in OCaml

- A number of libraries and frameworks are available for QuickCheck in OCaml

(some more polished than others...)

- This year we'll use the `QCheck` library

`https://github.com/c-cube/qcheck/`

Beware: The API changed with the 0.5 release

- The library is also available for installation through OPAM, OCaml's package manager

QuickCheck with QCheck

A QuickCheck test in QCheck needs 2 arguments:

- a generator (of random elements)
- a property (or specification / law)

For example:

```
let mytest =  
  Test.make float (fun f -> floor f <= f) ;;
```

where input is supplied by the **builtin float generator** `float` to test **the floor function** for the property
“**result of floor is less-or-equal than its argument**”.

We can now run it:

```
# QCheck_runner.run_tests [mytest] ;;  
success (ran 1 tests)
```

For the rest of today

We need to get you up and running in OCaml and QCheck:

So: install OCaml, QCheck, and an editor following the instructions

Once installed:

- try the selected exercises
- read the suggested chapters from Hickey's book